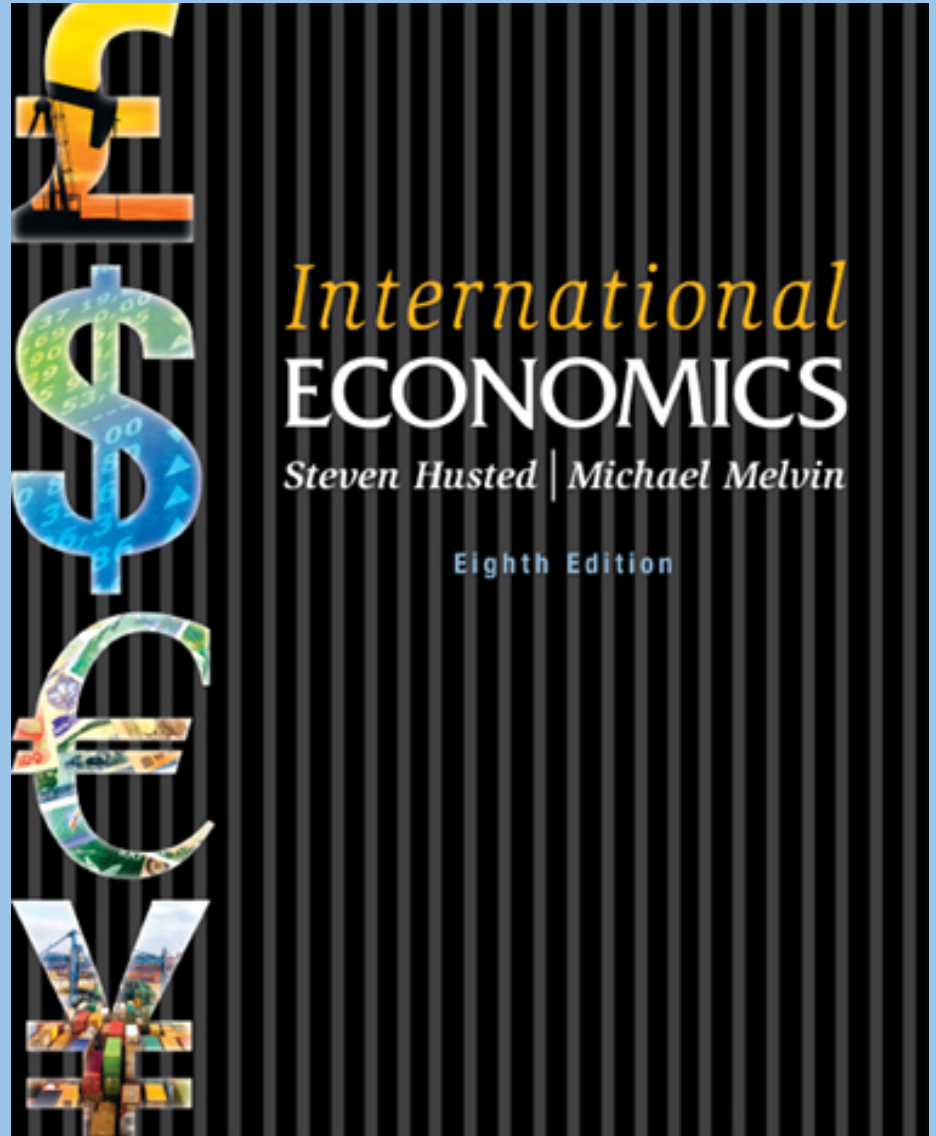


Chapter 15

Exchange Rates, Interest Rates, and Interest Parity: Adapted by Harris Dellas



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Topics to be Covered

- Interest Rate Parity
- Excess returns
- Real Interest Rate, Fisher Equation
- Exchange Rates, Interest Rates, and Inflation
- Expected Exchange Rates and the Term Structure of Interest Rates

Interest Parity



- The interest parity relationship is a result of profit-seeking arbitrage activity called **covered interest arbitrage**.
- A Swiss investor deciding between investing in CHFs or in USD must consider:
 - The interest rates, $i_{\$}$ and i_{CHF}
 - The spot exchange rate, S , (in CHF per USD)
 - The forward exchange rate, F , (in CHF per USD)

Interest Parity (cont.)



- By investing 1 CHF at home, the Swiss investor can earn $1 + i_{\text{CHF}}$ CHF after one period. Ex: $i_{\text{CHF}} = 10\%$ $1 \text{ CHF} \rightarrow 1.1 \text{ CHF}$
- Or, since $1 \text{ USD} = S \text{ CHF}$, the Swiss investor can convert 1 CHF into $1/S$ USD, invest in the USA and earn $(1/S) * (1 + i_{\$})$ USD
- Ex: $i_{\$} = 20\%$, $S=2$: 2 chf=1 USD, convert: 1 chf \rightarrow 0.5 usd, invest: 0.5 usd \rightarrow 0.6 usd ($0.5 * 1.2$)
- Since future spot rates are unknown, the investor can eliminate the uncertainty over the future CHF value of the investment with a forward exchange contract involving the forward rate, F. That is, by converting $(1 + i_{\$}) * (1/S)$ USD into $(1 + i_{\$}) * (1/S) * F$ CHF
- Ex: 1 usd = F chf, 0.6 usd = $0.6 * F$ chf

Covered Return



- **Covered return** is the domestic currency value of a foreign investment when the foreign currency proceeds are sold in the forward market for domestic currency.
- In our example, the covered return is equal to $(1 + i_{\$})F/S$ CHF. Arbitrage between the two investment opportunities results in $1 + i_{CHF} = (1 + i_{\$})*(F/S)$, that is,

$$\frac{1 + i_{CHF}}{1 + i_{\$}} = \frac{F}{S}$$

Ex: $1.1/1.2 = F/2 \rightarrow F = 2.2/1.2 = 1.83$ CHF is “expected” to appreciate (from 2 to 1.83)

Covered Interest Rate Parity



- Using $f = \log F$ and $s = \log S$ one can rewrite this equation as approximately

$$i_{CHF} - i_{\$} = \frac{F - S}{S} = f - s$$

Covered interest rate parity states that the forward premium (or discount) is equal to the interest differential.

:

Uncovered Interest Rate Parity



- If one chooses instead not to sell the foreign currency forward the *expected* return in CHF is $(1 + i_{\$}) \cdot (E_t S_{t+1} / S_t)$ where E denotes expectation. The two strategies are expected to yield -on average- the same return when **uncovered** IRP holds

$$\frac{1 + i_{CHF}}{1 + i_{\$}} = \frac{E_t S_{t+1}}{S_t}$$

- Or, approximately

$$i_{CHF} - i_{\$} = \frac{E_t S_{t+1} - S_t}{S_t} = E_t s_{t+1} - s_t$$



Excess returns, carry trade

- Excess return of keeping a risky position: $s_{t+1} - f_t$
- Carry trade: Borrow in the low interest rate currency (say CHF) and invest in the high interest rate currency (say, USD). Face future risk of exchange rate change.
- Return on carry trade, μ

$$\mu_t = S_{t+1}(1+i_{\$})/S_t - (1+i_{CHF}) \approx S_{t+1} - S_t + i_{\$} - i_{CHF}$$

- Profit from lower interest rate and if CHF depreciates (capital gain)

Carry Trade



EX: $i_{\text{CHF}} = 10\%$, $i_{\$} = 20\%$, $S(t) = 2$, $F(t) = 1.833$

- Borrow 1000 CHF at 10%, convert into 500 USD, invest at 20%, end up a year later with 600 USD.
- If $S(t+1) = F(t)$ then 600 USD are worth $600 * 1.833 = 1100$ CHF. Pay back loan+interest (1100 CHF), 0 profit from carry trade.
- If $S(t+1) = 2 > F(t)$ then 600 USD are worth $600 * 2 = 1200$ CHF. Pay back loan+interest (1100 CHF), 100 CHF profit from carry trade.
- If $S(t+1) = 1.6 < F(t)$ then 600 USD are worth $600 * 1.6 = 960$ CHF. Pay back loan+interest (1100 CHF), 140 CHF loss from carry trade.

Carry trade



- During the 2000s people outside CH were borrowing in CHF (and were buying assets in other currencies, e.g a house in Greece).
- A real example: A 20 year loan of 200000 CHF at 3% in 2006 (rather than at 5% in EUR). Monthly payment =1092 CHF.
- From 1998-2006, average CHF/EUR rate ≈ 1.5 .
- At that rate, need $1092/1.5 = 728$ EUR per month.
- Now the CHF/EUR=1.1. Need 993 EUR per month, 36% more!
- Had the CHF/EUR rate stayed at its historical average, the carry trade would have produced a profit of $880-728=152$ EUR per month (880 would have been the monthly payment on the equivalent EUR loan of $133333 \text{ EUR} = 200000/1.5 \text{ EUR}$).

Tests of excess returns



- If the forward rate is an unbiased predictor of future exchange rate, i.e. on average $s_{t+1} = f_t$, then the expected *average* excess return (or, the return to carry trade), $s_{t+1} - f_t$ is zero as $E_t s_{t+1} = f_t = s_t^* (1 + i_{CHF}) / (1 + i_{\$})$
- If it is not zero. Can the excess return from t to $t+1$ be predicted by some variable whose value is known at time t such as the carry?
- Excess Return: $ER_t = a + b^* \mu_t + u_t$ $\mu_t = s_{t+1} - s_t + i_{\$} - i_{CHF}$
- Or, equivalently (the famous Fama regression)
- $s_{t+1} - s_t = c + d^*(i_{CHF} - i_{\$}) + u_t$
- Test of no excess returns: $c = 0$; $d = 1$



Tests of excess returns (cont'd)

- All tests indicate that excess return is non zero and that $d < 1$ and often < 0 , that is, the carry trade is profitable.
- Enjoy -on average- higher interest rates and capital gains too!

- Explanations for this result:

- The excess return is compensation for higher risk

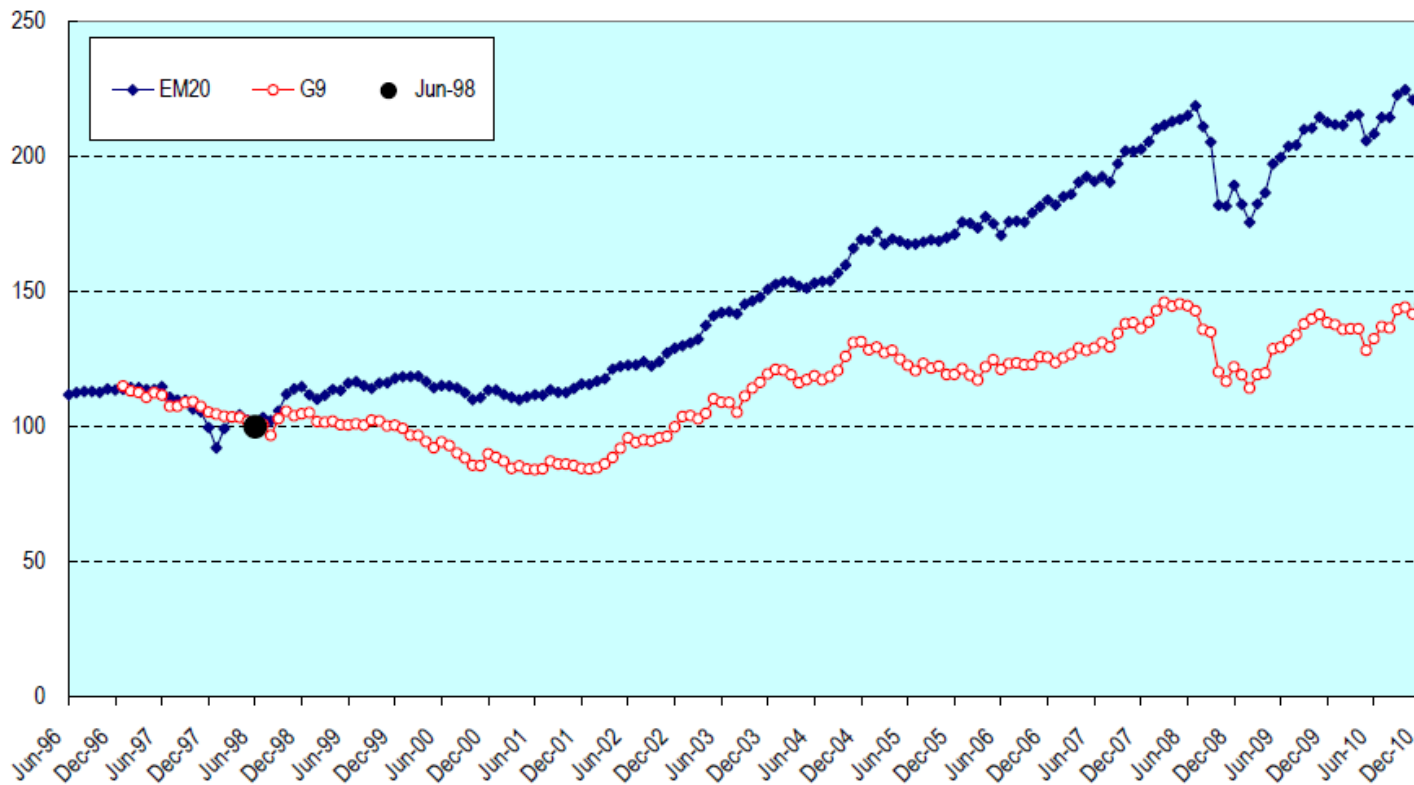
Choice between 100 and 0 and 200 with coin toss (prob=0.5). The expected value of this lottery is 100? Will its price be 100? No if people are risk averse.

- The excess return is due to irrationality, biases in forecasts, etc.



Figure 1: Cumulative USD Excess Returns, EM 20 and G9, June 1996 - December 2010

June 1998 value is set to 100



Interest Rates and Inflation



- **Nominal Interest Rate**—the interest rate actually observed in the market.
- **Realized –ex post- Real Interest Rate (RRIR)**—the nominal interest rate minus the inflation rate.
- **Expected –ex ante- Real Interest Rate (ERIR)**—the nominal interest rate minus expected inflation.
- ERIR is the more important concept as it is used as the basis for economic decisions.

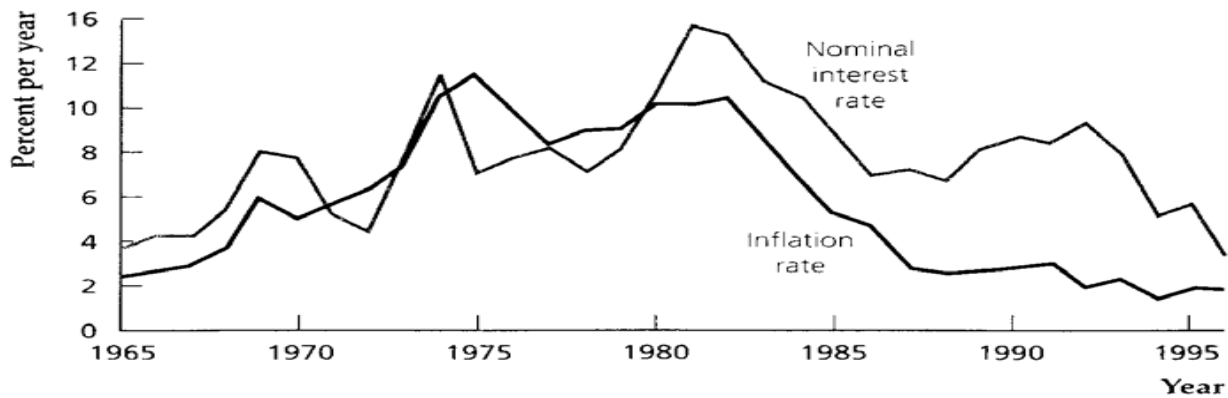


Fisher Equation

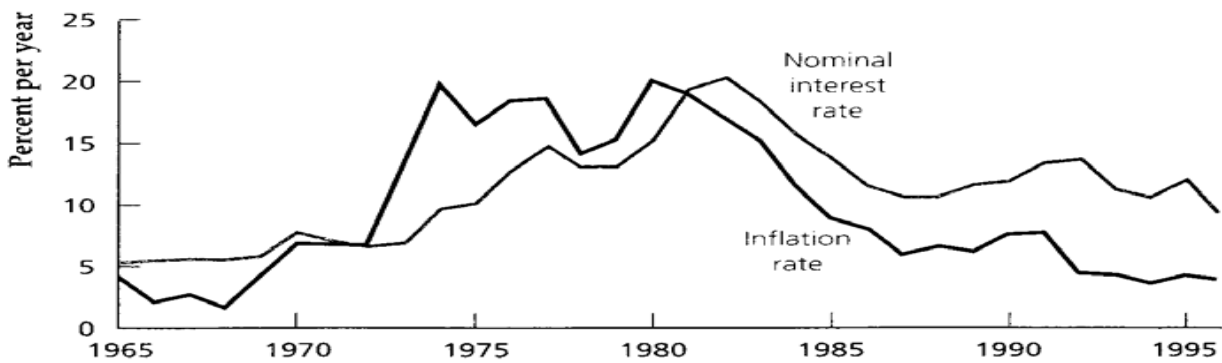
- The relationship between ex ante real interest rates and inflation is given by the **Fisher equation**:

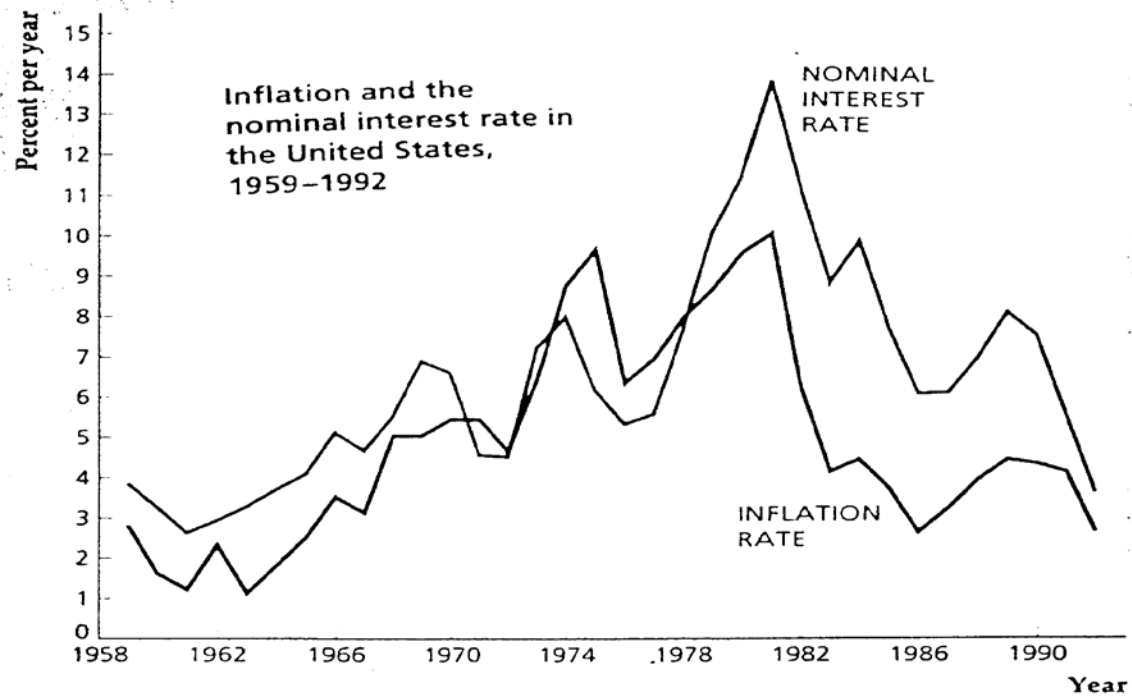
$$i = r + \pi^e$$

where i is the nominal interest rate, r is the real interest rate, and π^e is the expected rate of inflation.



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Interest Rates, Exchange Rates, and Inflation



- Ex ante real interest rates are equalized across countries when the Fisher equation, uncovered interest rate parity, and relative purchasing power parity all hold.

$$r_{CHF} - r_{\$} = i_{CHF} - i_{\$} - (\pi_{CH}^e - \pi_{US}^e) = f(t) - s(t) - (E_t s(t+1) - s(t))$$

- Interest rates, inflationary expectations, and exchange rates are all jointly determined and affected by government policy changes and other news.

Interest rates and the exchange rate: Another perspective



- Real interest rates and exchange rates
- We have used IRP to argue that if country A's nominal interest rate is higher than that in B, then A's currency will become weaker (depreciate).
- In the real world, we often hear that an increase in the nominal interest rate typically strengthens (appreciates) a currency.
- The distinction between different sources of changes in nominal interest rates (Fisher equation):

real interest rate (r) vs expected inflation (π^e)

$r \uparrow \Rightarrow s \downarrow$ (appreciation) $\pi^e \uparrow \Rightarrow s \uparrow$ (depreciation)

(s is the exchange rate chf/usd)

Real Interest Rates and Exchange Rates (cont'ed)



- Empirical evidence
- In low inflation environments an increase in the nominal interest rates is typically associated with a currency appreciation. The opposite in high inflation environments.
- Applications for CH monetary policy:
- Quantitative easing (QE) in the Eurozone and the abandonment of the CHF/EUR floor
- The use of negative interest rates in CH

Term Structure of Interest Rates



- There is no such thing as *the* interest rate for a country. Many interest rates
- **Term structure of interest rates**—the pattern of interest rates over different terms of maturity.
- Theories of the –slope- of term structure:
- the **Expectations Hypothesis** different term bonds can be viewed as a series of 1-period bonds.
- **Market Segmentation Theory**
- Interpretation of slope

Expected Exchange Rates and Term Structure of Interest Rates



- Refer to Figure 15.1 Eurocurrency Interest Rates
- If the term structure lines for two countries are:
 - Parallel, then exchange rate changes are expected to be constant
 - Diverging, then the high-interest-rate currency is expected to depreciate at an increasing rate over time
 - Converging, then the high-interest-rate currency is expected to depreciate at a declining rate relative to the low-interest-rate currency

FIGURE 15.1 Eurocurrency Interest Rates for July 13, 2008

