

Law of One Price (Goods market)

PPP (absolut terms)

$$P_t = e_t P_t^*$$

PPP (relative terms)

Log-differentiate:

$$dP_t/P_t = de_t/e_t + dP_t^*/P_t^*$$

$$\pi_t \approx \hat{e}_t + \pi_t^*$$

XR (change)

$$\hat{e}_{t+1} = (e_{t+1} - e_t)/e_t$$

XR expectation parity

“Forward exchange rates mirror expected future spot rates.”

$$(f_t = E_t[e_{t+1}])$$

UIRP

$$\begin{aligned} 1 + i_t &= (1 + i_t^*) E_t[e_{t+1}]/e_t \\ &= (1 + i_t^*) + (E_t[e_{t+1}]/e_t - 1) + \underbrace{i_t^* (E_t[e_{t+1}]/e_t - 1)}_{small} \end{aligned}$$

$$i_t \approx i_t^* + E_t[\hat{e}_{t+1}]$$

Forward XR

$$E_t[\hat{e}_{t+1}] = E_t[(e_{t+1} - e_t)/e_t] = f_t/e_t - 1$$

Inflation differential

$$\pi_t - \pi_t^*$$

Interest rate differential

$$i_t - i_t^*$$

National Fisher parity:

$$1 + r_t = (1 + i_t)/(1 + \pi_t)$$

$$\log: r_t \approx i_t - \pi_t$$

International Fisher parity

$$\frac{(1 + r_t^*)}{(1 + r_t)} = \frac{(1 + i_t^*)(1 + \pi_t)}{(1 + \pi_t^*)(1 + i_t)}$$

$$\log: r_t^* - r_t \approx (\pi_t - \pi_t^*) - (i_t - i_t^*)$$

Law of One Price
(Capital market)

CIRP

$$\begin{aligned} 1 + i_t &= (1 + i_t^*) f_t/e_t \\ &= (1 + i_t^*) + (f_t/e_t - 1) + \underbrace{i_t^* (f_t/e_t - 1)}_{small} \end{aligned}$$

$$i_t \approx i_t^* + (f_t - e_t)/e_t$$

$$\log: i_t - i_t^* \approx f_t - e_t$$