

## 6. The Labor Market

### Problem 6.1.

Consider an economy with many identical households. Each household owns a business that employs both capital (machinery)  $k$  and labour  $l_d$  to produce output  $y$ . (The “d” is for demand.) Production possibilities are represented by  $y = Z \cdot k^{0.3} l_d^{0.7}$

The stock of capital that each household owns is fixed. It may employ labour at the prevailing wage  $w$  per unit of labour  $l_d$ . Each household takes the wage as given. The profit of each household from running its business is:

$$\pi = y - w l_d = Z \cdot k^{0.3} l_d^{0.7} - w l_d$$

a) Determine the optimal amount of labor for each household to hire as a function of its capital endowment  $k$  and the prevailing wage  $w$ . Call this amount of labor  $l_d^*$  ?

b) What is the maximized profit of the household?

c) Each household has preferences over its consumption  $c$  and labor supply  $l_s$ . These preferences are represented by the utility function  $u(c, l_s) = c^{0.5} (1 - l_s)^{0.5}$

Each household has an endowment of labor can be used in the household's own business or rented to others at the wage  $w$ . If the household supplies labor  $l_s$ , then it will earn labor income  $w \cdot l_s$ . Output, wages, and profit are all quoted in terms of real goods, so they can be consumed directly. Set up the household's problem for choosing its labor supply  $l_s$ .

d) Carry out the maximization from part c) to derive the optimal labor supply  $l_s$

e) Determine the equilibrium wage  $w^*$  in this economy.

f) How does the equilibrium wage  $w^*$  change with the amount of capital  $k$  owned by each household?

### Exercise 6.2.

This question concerns an economy with two types of agents: capitalists and workers. There are 1000 capitalists, each of whom owns a farm. A capitalist does not work; he consumes all of his profits immediately. Each farm has the technology:

$$c = 2\sqrt{n}$$

There are 1000 workers. Each worker owns no land, but he is endowed with 1 unit of labor. Workers work for capitalists at a market-determined real wage  $w$ . A worker consumes all of his wage income immediately; he has no source of income other than wages. Each worker has preferences over goods consumption  $c$  and labor supplied  $n$  of the form:

$$u(c, n) = \log c + \log(1 - n)$$

- (a) What is the demand for labor in this economy?
- (b) What is the supply of labor in this economy?
- (c) What is the equilibrium wage rate?

**Problem 6.3.** (Barro 6.6: The Labor market and efficiency)

In the text we considered two isolated regions, A and B. The technology in A was inferior to that in B. Therefore, we found that opening up, of an economy-wide labor market led to higher aggregate output without requiring an increase in aggregate work effort. In this sense the new market improved the economy's efficiency.

- a) Does the result mean that everybody is better off? In answering, consider the position of workers and firms (and the owners of the firms) in both regions.
- b) Does your answer suggest that some groups might oppose moves to free up markets, even when there would be gains in the aggregate? Can you think of any real-world examples of this phenomenon?